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US Particle Accelerator School
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LLNL: UCRL-?TBD?
LBNL: LBNL-?TBD?

"Beam Physics with Intense Space Charge"

Lecturers:
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Lawrence Livermore National Laboratory
Lawrence Berkeley National Laboratory

Grader:
Mikhail Dorf
Lawrence Livermore National Laboratory

Class material including a course overview, lecture schedule, a more detailed course description, lecture notes (pdf copies), problems sets, and the final exam can be found on the course web site:

http://hifweb.lbl.gov/USPAS_2011

Topical Course Outline:

"Beam Physics with Intense Space-Charge"

Note: This outline and the distribution files are arranged in logical presentation order. In the actual class, there were deviations from this order due to practical constraints. The actual order of material presented is given in the lecture schedule on the course web site.

Lecturer abbreviations:

JJB - J.J. Barnard
SML - S.M. Lund

1. Introduction to the Physics of Beams and Basic Parameters (JJB)
 - 1.1 Particle equations of motion
 - 1.2 Dimensionless parameters: Perveance, phase advance, space charge tune depression
 - 1.3 Plasma physics of beams: collisions, Debye Length
 - 1.4 Klimontovich equation, Vlasov equation, Liouville's theorem
 - 1.4 Emittance and brightness
2. Envelope Equations-I (JJB)
 - 2.1 Paraxial Ray Equation
 - 2.2 Envelope equations for axially symmetric beams
 - 2.3 Cartesian equations of motion
 - 2.3.1 Quadrupole focusing
 - 2.3.2 Space charge force for elliptical beams
 - 2.4 Envelope equations for elliptically symmetric beams
3. Current Limits in Accelerators and Centroid equations-I (JJB)
 - 3.1 Axisymmetric beams
 - 3.1.1 Solenoids
 - 3.1.2 Einzel Lenses
 - 3.2 Elliptically symmetric beams
 - 3.2.1 Derivation of space charge term in envelope equation with elliptical symmetry
 - 3.2.2 Current limit for quadrupoles using Fourier transforms
 - 3.3 Current limit for continuous focusing
 - 3.3.1 Calculation of σ_0 (using matrix multiplication)
 - 3.3.2 Comparison of quadrupole current limit (from Fourier transform, and matrix methods)
 - 3.4 Centroid equations (first order moments)
 - 3.4.1 Space charge and focusing forces

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3.5 Image forces (effect on centroid and envelope)

4. Transverse Particle Dynamics (SML)
 - 4.1 Particle Equations of Motion
 - 4.1.A Introduction: The Lorentz Force Equation
 - 4.1.B Applied Fields
 - 4.1.C Machine Lattice
 - 4.1.D Self Fields
 - 4.1.E Equations of Motion in s and the Paraxial Approximation
 - 4.1.F Summary: Transverse Particle Equations of Motion
 - 4.1.G Overview of Analysis to Come
 - 4.1.H Bent Coordinate System and Particle Equations of Motion with Dipole Bends and Axial Momentum Spread
 - 4.2 Transverse Particle Equations of Motion in Linear Focusing Channels
 - 4.2.A Introduction
 - 4.2.B Continuous Focusing
 - 4.2.C Alternating Gradient Quadrupole Focusing - Electric Quadrupoles
 - 4.2.D Alternating Gradient Quadrupole Focusing - Magnetic Quadrupoles
 - 4.2.E Solenoidal Focusing
 - 4.2.F Summary of Transverse Particle Equations of Motion
 - Appendix A: Quadrupole Skew Coupling
 - Appendix A: The Larmor Transform to Express Solenoidal Focused Particle Equations of Motion in Uncoupled Form
- 4.3 Description of Applied Focusing Fields
 - 4.3.A Overview
 - 4.3.B Magnetic Field Expansions for Focusing and Bending
 - 4.3.C Hard Edge Equivalent Models
 - 4.3.D 2D Transverse Multipole Magnetic Moments
 - 4.3.E Good Field Radius
 - 4.3.F Example Permanent Magnet Assemblies
- 4.4 Transverse Particle Equations of Motion with Nonlinear Applied Fields
 - 4.4.A Overview
 - 4.4.B Approach 1: Explicit 3D Form
 - 4.4.C Approach 2: Perturbed Form
- 4.5 Linear Equations of Motion Without Space-Charge, Acceleration, and Momentum Spread
 - 4.5.A Hill's equation
 - 4.5.B Transfer Matrix Form of the Solution to Hill's Equation
 - 4.5.C Wronskian Symmetry of Hill's Equation
 - 4.5.D Stability of Solutions to Hill's Equation in a Periodic Lattice
- 4.6 Hill's Equation: Floquet's Theorem and the Phase-Amplitude Form of the Particle Orbit
 - 4.6.A Introduction
 - 4.6.B Floquet's Theorem
 - 4.6.C Phase-Amplitude Form of the Particle Orbit
 - 4.6.D Summary: Phase-Amplitude Form of the Solution to Hill's Equation
 - 4.6.E Points on the Phase-Amplitude Formulation
 - 4.6.F Relation Between the Principal Orbit Functions and the Phase-Amplitude Form Orbit Functions
 - 4.6.G Undepressed Particle Phase Advance
- Appendix C: Calculation of $w(s)$ from Principal Orbit Functions
- 4.7 Hill's Equation: The Courant-Snyder Invariant and the Single-Particle Emittance
 - 4.7.A Introduction
 - 4.7.B Derivation of the Courant-Snyder Invariant
 - 4.7.C Lattice Maps
- 4.8 Hill's Equation: The Betatron Formulation of the Particle Orbit and Maximum Orbit Excursions
 - 4.8.A Formulation
 - 4.8.B Maximum Orbit Excursions
- 4.9 Momentum Spread Effects and Bending
 - 4.9.A Overview
 - 4.9.B Chromatic Effects
 - 4.9.B Dispersive Effects
- 4.10 Acceleration and Normalized Emittance
 - 4.10.A Introduction
 - 4.10.B Transformation to Normal Form
 - 4.10.C Phase-Space Relations Between Transformed and Untransformed Systems
- Appendix D: Accelerating Fields and Calculation of Changes in $\gamma\beta$

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	Contact Information References Acknowledgments	
5.	Transverse Equilibrium Distribution Functions (SML)	
5.1	Vlasov Model	
	Vlasov-Poisson System Review: Lattices: Continuous, Solenoidal, and Quadrupole Review: Undepressed Particle Phase Advance	
5.2	Vlasov Equilibria	
	Equilibrium Conditions Single Particle Constants of the Motion Discussion: Plasma Physics Approach to Beam Physics	
5.3	The KV Equilibrium Distribution	
	Hill's Equation with Linear Space-Charge Forces Review: Courant-Snyder Invariants Courant-Snyder Invariants for a Uniform Density Elliptical Beam KV Envelope Equations Canonical Form of the KV Distribution Function Matched Envelope Structure Depressed Particle Orbits rms Equivalent Beams Discussions/Comments on the KV Model	
	Appendix A: Self-Fields of a Uniform Density Elliptical Beam in Free Space (handwritten notes) Derivation #1: Direct Derivation #2: Simplified	
	Appendix B: Canonical Transforms of the KV Distribution (handwritten notes) Canonical Transforms Simplified Moment Calculations	
5.4	The Continuous Focusing Limit of the KV Distribution	
	Reduction of Elliptical Model Wavenumbers of Particle Oscillations Distribution Form Discussion	
5.5	Continuous Focusing Equilibrium Distributions	
	Equilibrium Form Poisson's Equation Moments and rms Equivalent Beam Envelope Equation Example Distributions	
5.6	Continuous Focusing: The Waterbag Equilibrium Distribution	
	Distribution Form Poisson's Equation Solution in Terms of Accelerator Parameters Equilibrium Properties	
5.7	Continuous Focusing: The Thermal Equilibrium Distribution	
	Overview Distribution Form Poisson's Equation Solution in Terms of Accelerator Parameters Equilibrium Properties	
5.8	Continuous Focusing: Debye Screening in a Thermal Equilibrium Beam	
	Poisson's Equation for the Perturbed Potential Due to a Test Particle Solution for Characteristic Debye Screening	
5.9	Continuous Focusing: The Density Inversion Theorem	
	Relation of Density Profile to the Full Distribution Function Example Application to the KV Distribution	
5.10	Comments on the Plausibility of Smooth, non-KV Vlasov Equilibria in Periodic Focusing Lattice	
	Discussion Contact Information References Acknowledgments	
6.	Transverse Particle Resonances with Application to Circular Accelerators (SML)	
6.1	Overview	
	Hill's Equation Review: Betatron Form of Phase-Amplitude Solution	

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	Transform Approach Random and Systematic Perturbations Acting on Orbits	
6.2	Floquet Coordinates	
	Transformation of Hill's Equation to a Simple Harmonic Oscillator Phase-Space Structure of Solution Expression of the Courant-Snyder Invariant Phase-Space Area Transform	
6.3	Perturbed Hill's Equation in Floquet Coordinates	
	Transformation Result for x-Equation	
6.4	Sources and Forms of Perturbation Terms	
	Power Series Expansion of Perturbations Connection to Multipole Errors	
6.5	Perturbed Solution: Resonances	
	Fourier Expansion of Perturbations and Resonance Terms Resonance Conditions	
6.6	Machine Operating Points: Restrictions Resulting from Resonances	
	Tune Restrictions from Low Order Resonances	
6.7	Space-Charge Effects	
	Coherent and Incoherent Tune Shifts Laslett Limit	
	Contact Information References Acknowledgments	
7.	Injectors and Longitudinal Physics Part I (JJB)	
7.1	Diodes and Injectors	
7.1.1	Space-charge limited flow and child-Langmuir law	
7.1.2	Pierce electrodes	
7.1.3	Transients in injectors and Lampel-Tiefenback solution	
7.2	Injector Choices	
8.	Longitudinal Physics Part II (JJB)	
8.1	Acceleration -- introduction	
8.2	Space charge of short bunches (in rf-accelerators)	
8.3	Space charge of long bunches (g-factor model)	
8.4	Longitudinal 1D Vlasov equation	
8.5	Longitudinal fluid equation	
8.4	Longitudinal space charge waves	
8.5	Longitudinal rarefaction waves and bunch end control	
9.	Longitudinal Physics Part III (JJB)	
9.1	Longitudinal cooling from acceleration	
9.2	Longitudinal resistive instability	
9.3	Bunch compression	
9.4	Longitudinal envelope equation	
9.4	Neuffer distribution function	
10.	Transverse Centroid and Envelope Descriptions of Beam Evolution (SML)	
10.1	Overview	
10.2	Derivation of Centroid and Envelope Equations of Motion	
	Statistical Averages Particle Equations of Motion Distribution Assumptions Self-Field Calculation: Direct and Image Coupled Centroid and Envelope Equations of Motion	
10.3	Centroid Equations of Motion	
	Single Particle Limit: Oscillation and Stability Properties Effect of Driving Errors Effect of Image Charges	
10.4	Envelope Equations of Motion	
	KV Envelope Equations Applicability of Model Properties of Terms	
10.5	Matched Envelope Solutions	
	Construction of Matched Solution Symmetries of Matched Envelope: Interpretation via KV Envelope Equations Examples	
10.6	Envelope Perturbations	
	Perturbed Equations	

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Matrix Form: Stability and EigenMode Symmetries
 Decoupled Modes
 General Mode Limits
 10.7 Envelope Modes in Continuous Focusing
 Normal Modes: Breathing and Quadrupole Modes
 Driven Modes
 10.8 Envelope Modes in Periodic Focusing Channels
 Solenoidal Focusing
 Quadrupole Focusing
 Mode Launching
 10.9 Transport Limit Scaling Based on Envelope Models
 (see handwritten notes)
 Overview
 Example Calculation for a Periodic FODO Quadrupole Transport Channel
 Discussion on Application of Formulas in Design
 Results of More Detailed Models
 10.10 Centroid and Envelope Descriptions via
 1st Order Coupled Moment Equations
 Formulation
 Example Illustration - Familiar KV Envelope Model
 Contact Information
 References
 Acknowledgments

11. Continuous Focusing Envelope Modes and Beam Halo (JJB)
 11.1 Envelope modes of unbunched beams in continuous focusing
 11.2 Envelope modes of bunched beams in continuous focusing
 11.3 Halos from mismatched beams
 11.3.1 What is halo? Why do we care
 11.3.2 Qualitative picture of halo formation: mismatches
 resonantly drive particles to large amplitude
 11.3.3 Core/particle models
 11.3.4 Amplitude phase analysis

12. Transverse Kinetic Stability (SML)
 12.1 Overview: Machine Operating Points
 Notions of Beam Stability
 Tiefenback Experimental Results for Quadrupole Transport
 12.2 Overview: Collective Modes and Transverse Kinetic Stability
 Possibility of Collective Internal Modes
 Vlasov Model Review
 Plasma Physics Approach to Understanding Higher Order Instability
 12.3 Linearized Vlasov Equation
 Equilibrium and Perturbations
 Linear Vlasov Equation
 Method of Characteristics
 Discussion
 12.4 Collective Modes on a KV Equilibrium Beam
 KV Equilibrium
 Linearized Equations of Motion
 Solution of Equations
 Mode Properties
 Physical Mode Components Based on Fluid Model
 Periodic Focusing Results
 12.5 Global Conservation Constraints
 Conserved Quantities
 Implications
 12.6 Kinetic Stability Theorem
 Effective Free Energy
 Free Energy Expansion in Perturbations
 Perturbation Bound and a Sufficient Condition for Stability
 Interpretation and Example Applications
 12.7 rms Emittance Growth and Nonlinear Forces
 Equations of Motion
 Coupling of Nonlinear Forces to rms Emittance Evolution
 12.8 rms emittance Growth and Nonlinear Space-Charge Forces
 Equations of Motion
 rms Equivalent Beam Forms
 Wangler's Theorem

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12.9 Uniform Density Beams and Extreme Energy States
 Variational Formulation
 Self-Field Energy Minimization
 12.10 Collective Relaxation and rms Emittance Growth
 Conservation Constraints
 Relaxation Processes
 Emittance Growth Bounds from Space-Charge Nonuniformities
 12.11 Halo Induced Mechanism of Higher-Order Instability
 Halo Model for an Elliptical Beam
 Pumping Mechanism
 Stability Properties
 12.12 Phase Mixing and Landau Damping in Beams
 (to be added in future versions)
 Contact Information
 References
 Acknowledgments

13. Pressure, Scattering, and Electron Effects (JJB)
 13.1 Beam/beam Coulomb collisions
 13.2 Beam/residual-gas scattering
 13.3 Charge-changing processes
 13.4 Wall effects
 13.4.1 gas pressure instability
 13.5 Electron cloud processes
 13.5.1 Multiple-bunch beam-induced multipacting
 13.5.2 Single-bunch beam-induced multipacting
 13.6 Electron-ion instability

14. Heavy Ion Fusion and Final Focus (JJB)
 14.1 An application of intense beams: Heavy Ion Fusion
 14.1.1 Requirements
 14.1.2 Targets for inertial confinement fusion
 14.1.3 Accelerator
 14.1.4 Drift compression
 14.1.5 Final focus
 14.2 Final focus
 14.2.1 Predicting spot size using envelope equation
 and estimate of effects from chromaticity
 14.3 Experiments for Heavy Ion Fusion

15. Numerical Simulations (SML)
 15.1 Why Numerical Simulation?
 15.2 Classes of Intense Beam Simulations
 15.2.A Overview
 15.2.B Particle Methods
 15.2.C Distribution Methods
 15.2.D Moment Methods
 15.2.E Hybrid Methods
 15.3 Overview of Basic Numerical Methods
 15.3.A Discretizations
 15.3.B Discrete Numerical Operations
 - Derivatives
 - Quadrature
 - Irregular Grids and Axisymmetric Systems
 15.3.C Time Advance
 - Overview
 - Euler and Runge-Kutta Advances
 - Solution of Moment Methods
 15.4 Numerical Methods for Particle and Distribution Methods
 15.4.A Overview
 15.4.B Integration of Equations of Motion
 - Leapfrog Advance for Electric Forces
 - Leapfrog Advance for Electric and Magnetic Forces
 - Numerical Errors and Stability of the Leapfrog Method
 - Illustrative Examples
 15.4.C Field Solution
 - Electrostatic Overview
 - Green's Function Approach
 - Gridded Field Solution: Equation and Boundary Conditions

- Methods of Gridded Field Solution
 - Spectral Methods and the FFT
 - 15.4.D Weighting: Depositing Particles on the Field Mesh and Interpolating Fields to the Particles
 - Overview of Approaches
 - Approaches: Nearest Grid Point, Cloud in Cell, Area, Splines
 - 15.4.E Computational Cycle for Particle in Cell Simulations
 - 15.5 Diagnostics
 - 15.6 Initial Distribution and Particle Loading
 - 15.7 Numerical Convergence
 - 15.8 Practical Considerations
 - 15.8.A Overview
 - 15.8.B Fast Memory
 - 15.8.C Run Time
 - 15.8.D Machine Architectures
 - 15.9 Overview of the WARP Code
 - 15.10 Example Simulations
 - Contact Information
 - Acknowledgments
 - References
16. Summary of Lectures by John J. Barnard (JJB)
- 16.1 Emittance and phase space review
 - 16.2 Particle equations of motion (radial and Cartesian)
 - 16.3 Summary of 6 statistical envelope equations and two equations based on particular distribution functions
 - 16.4 Current limits
 - 16.5 Using envelope equations to estimate spot size
 - 16.6 Longitudinal dynamics summary
 - 16.7 Instability summary
 - 16.8 Halo summary
 - 16.9 Electron, gas, pressure, and scattering effects summary
 - 16.10 Summary of HIF